$$\left(1+\frac{3x}{2}\right)^8$$

$$(a+b)^8 = a^8 + 8a^7b + {8 \choose 2}a^6b^2 + {8 \choose 3}a^5b^3$$

$$(3x) + 28(3x)^2 + 56(3x)^3$$

$$8(\frac{3x}{2}) + 28(\frac{3x}{2})^2 + 56(\frac{3x}{2})^3$$

$$3(\frac{3x}{2}) + 28(\frac{3x}{2})^2 + 56(\frac{3x}{2})^3$$

$$=1+12x+63x^2+189x^3$$

$$(1+\frac{3x}{2})^8 = 1+8(\frac{3x}{2})+28(\frac{3x}{2})^2+56(\frac{3x}{2})^3$$

Leave

Given that the fourth term of this series is 62.5

(a) Show that $r = \frac{5}{3}$

(b) find the value of a,

2. A geometric series has first term a, where $a \neq 0$, and common

The sum to infinity of this series is 6 times the first term of the

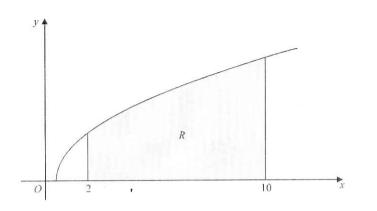
$$\frac{6a}{6a} = \frac{1}{6a}$$

b)
$$U_4 = \alpha r^3 = \alpha (\frac{5}{2})^3 = 62.5 \therefore \alpha = 108.$$

$$S_{30} = 108(1 - (\frac{5}{6})^{30}) = 645.27...$$

c)
$$S_{30} = 108\left(1 - \left(\frac{\xi}{\xi}\right)^{30}\right) = 645.27...$$

 $\frac{1}{\xi}$
=: difference = $\frac{108}{(\frac{1}{\xi})} - 645.27...$



3.

Figure 1

Figure 1 shows a sketch of part of the curve with equation $y = \sqrt{(2x-1)}$, $x \ge 0.5$

The finite region R, shown shaded in Figure 1, is bounded by the curve, the x-axis and the lines with equations x = 2 and x = 10.

The table below shows corresponding values of x and y for $y = \sqrt{(2x - 1)}$.

| | | -) h=2 | | | | |
|---|----|--------|-----|-----|-----|--|
| x | 2 | 4 | 6 | 8 | 10 | |
| y | √3 | 17 | √11 | Vis | V19 | |

(a) Complete the table with the values of y corresponding to x = 4 and x = 8.

(1)

(b) Use the trapezium rule, with all the values of y in the completed table, to find an approximate value for the area of R, giving your answer to 2 decimal places.

(3)

(c) State whether your approximate value in part (b) is an overestimate or an underestimate for the area of R.

for the area of R.

Areu
$$\stackrel{\circ}{=} \frac{1}{2} (2) \left[\sqrt{3} + 2 \left(\sqrt{7} + \sqrt{11} + \sqrt{15} \right) + \sqrt{19} \right] = 25.76$$

conder estimate, trapezia will be below curve

blank

(a) find the value of a,

Given that (x-2) is a factor of f(x),

(b) factorise f(x) completely.

 $a(x) = -4x^3 + ax^2 + 9x - 16,$ $a(x) = -4x^3 + ax^2 + 6x - 16,$ $a(x) = -4x^3 +$

(c) find the remainder when f(x) is divided by (2x-1).

a) f(z)=0 => -32+4a+18-18=0

 \boldsymbol{x}

 $= -(\infty - 2)(4x^2 - 9)$ = -(x-2)(2x-3)(2x+3)

c) $f(\frac{1}{2}) = -4(\frac{1}{8}) + 8(\frac{1}{4}) + 9(\frac{1}{2}) - 18 = -12$

: remainder is -12

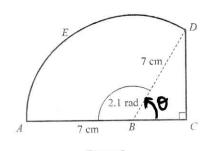


Figure 2

Figure 2 shows the shape ABCDEA which consists of a right-angled triangle BCD joined to a sector ABDEA of a circle with radius 7 cm and centre B.

A, B and C lie on a straight line with AB = 7 cm.

Given that the size of angle ABD is exactly 2.1 radians,

(a) find, in cm, the length of the arc DEA,

 $\theta = \Pi - 2.1$

(b) find, in cm, the perimeter of the shape ABCDEA, giving your answer to 1 decimal place.

a)
$$arc = r\theta = 7 \times 2.1 = 14.7$$

BC =
$$7(0s(\pi-2.1) = 3.53$$

$$P = 7 \sin(\pi - 2.1) = 6.04$$



6.

(2)

(4)



The curve C has a maximum turning point at the point A and a minimum turning point at

Figure 3 shows a sketch of part of the curve C with equation

$$y = \frac{1}{8}x^3 + \frac{3}{4}x^2, \quad x \in \mathbb{R}$$

the origin O. The line I touches the curve C at the point A and cuts the curve C at the point B.

The x coordinate of A is -4 and the x coordinate of B is 2.

The finite region R, shown shaded in Figure 3, is bounded by the curve C and the line l.

Use integration to find the area of the finite region
$$R$$
.

(7)

$$\alpha = 2 \quad y = \frac{1}{2}(x) + \frac{3}{4}(4) = 4$$

$$R = 24 - \int \frac{1}{8}x^3 + \frac{3}{4}x^2 dx$$

$$= 24 - \left[\frac{1}{32}x^4 + \frac{3}{2}x^3\right]_{-4}^{2}$$

$$= 24 - \left[\left(\frac{5}{4}\right) - \frac{1}{4}\right]_{-4}^{2}$$

(3)

$$\frac{\sin 2\theta}{(4\sin 2\theta - 1)}$$

(ii) Solve, for
$$0 \le x < 2\pi$$
, the equation

7. (i) Solve, for $0 \le \theta \le 180^{\circ}$, the equation

$$5\sin^2 x - 2\cos x - 5 = 0$$

i) Sin 20 = 4 Sin 20 -1 => 3 Sin 20 =1

ii)
$$5(1-(\cos^2 x)-2(\cos x-5=0)$$

$$x = \frac{1.98}{2}$$
 $x = 1.98$, 4.30

8. (i) Solve

' (ii) Use algebra to find the values of x for which

$$\log_2(x+15) - 4 = \frac{1}{2}\log_2 x$$

$$x=22S \qquad x=1$$

$$x+15=16\sqrt{2}$$

 $x-16\sqrt{2}+15=0$
 $(\sqrt{2}x-15)(\sqrt{2}x-1)=0$

ii)
$$\log_2(x+is) - \log_2(\sqrt{x}) = 4$$

5y = 8

Figure 4 shows the plan of a pool. The shape of the pool ABCDEFA consists of a rectangle BCEF joined to an equilateral triangle BFA and a semi-circle CDE, as shown in Figure 4.

Given that AB = x metres, EF = y metres, and the area of the pool is 50 m²,

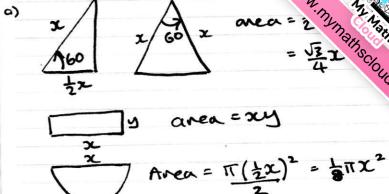
(a) show that

$$y = \frac{50}{x} - \frac{x}{8}(\pi + 2\sqrt{3})$$

(b) Hence show that the perimeter,
$$P$$
 metres, of the pool is given by

 $P = \frac{100}{x} + \frac{x}{4}(\pi + 8 - 2\sqrt{3})$

(c) Use calculus to find the minimum value of P, giving your answer to 3 significant figures.



$$xy + \frac{1}{8}\pi x^{2} + \frac{13}{4}x^{2} = 50$$

$$xy = 50 - \frac{1}{8}x^{2} (\pi - 2\sqrt{3})$$

:. y= 50 - \$x(11-2/3)

$$\rho = 2y + (2 + \frac{1}{2}\pi)x$$

Ouestion 9 continued

(3)

P=100-~~(11+2人3)+(2+効义

b= 100 + 5 (8+24-11-5/3)

P= 딸+즌(T+8-25) #

$$\rho' = 100 \times^{-1} + \left(\frac{11+8}{4} \frac{h_{M_{N_{1}}, N_{1}, N_{1}, N_{2}, N_{3}}}{4} \right) \frac{1}{4} = -100 \times^{-2} + \left(\frac{11+8-2\sqrt{3}}{4} \right) \frac{h_{M_{N_{1}}, N_{2}, N_{3}, N_{3},$$

=) $\chi^2 = \frac{400}{\pi + 8 - 2.5}$:- $\chi = 7.22$

:. Min
$$P = \frac{100}{7.22...} + \left(\frac{11+8-2\sqrt{3}}{4}\right)(7.22...)$$

Min $P = 27.7$

d) at x=7-22 P" = 200 >0

